Chapter 5 Thermochemistry

Thermodynamics and Thermochemistry
• Why do chemical reactions occur? One major driving force for reactions is stability: Substances that are high in energy are generally less stable and more reactive, while substances that are lower in energy are generally more stable and less reactive.
• Thermodynamics is the study of heat and its transformations.
• Thermochemistry is the branch of thermodynamics that deals with the relationships between chemistry and energy.

C(s) + O_2(g) → CO_2(g) + heat
2KClO_3(s) + heat → 2KCl(s) + 3O_2(g)

Energy, Work, and Heat
• Energy is the capacity to do work or to supply heat. Energy can be exchanged between objects by some combination of either heat or work:

\[ \Delta E = q + w \]

• Work is done when a force is exerted through a distance:

\[ \text{Work} = \text{force} \times \text{distance} \]

• Heat is the flow of energy caused by a temperature difference.

Heat flows from a region of higher temperature to a region of lower temperature, until the two regions reach the same temperature, and are at thermal equilibrium.

Energy and the First Law of Thermodynamics

Heat and Temperature
• Heat and temperature are not the same thing!
  – Heat is the exchange of thermal energy between a system and its surroundings. Temperature is a measure of the thermal energy of a sample.
  – A fresh cup of coffee is hotter than a swimming pool, but a swimming pool holds more heat than the coffee. If you pour a 200°F cup of coffee into a 100°F pool, the pool won’t become 150°F.
• All forms of energy can be converted quantitatively into heat, so it is possible to use heat as a measure of energy for any chemical or physical process.

Kinetic and Potential Energy
• Kinetic energy \( E_k \) is the energy due to the motion of an object with mass \( m \) and velocity \( v \):

\[ E_k = \frac{1}{2} mv^2 \]

– Thermal energy, the energy associated with the temperature of an object, is a form of kinetic energy, because it arises from the vibrations of the atoms and molecules within the object.
• Potential energy \( E_p \) is energy due to position, or any other form of “stored” energy. There are several forms of potential energy:
  – Gravitational potential energy \( E_p = mgh \)
  – Mechanical potential energy
  – Chemical potential energy (stored in chemical bonds)
**Kinetic and Potential Energy**

- Potential energy *increases* when things that attract each other are separated or when things that repel each other are moved closer.
- Potential energy *decreases* when things that attract each other are moved closer, or when things that repel each other are separated.
- According to the law of conservation of energy, energy cannot be created or destroyed, but can be converted from one form to another.

**Units of Energy**

- From the expression for kinetic energy it can be seen that energy has units of \( \text{kg} \cdot \text{m}^2/\text{s}^2 \) (kg m\(^2\) s\(^{-2}\)).
- The SI unit of energy is the *joule* (J): 
  \[
  1 \text{ J} = 1 \text{ kg} \text{ m}^2/\text{s}^2
  \]
- A *calorie* (cal) is the amount of energy needed to raise the temperature of 1 g of water by 1 °C. 
  \[
  1 \text{ cal} = 4.184 \text{ J (exact)}
  \]
- The nutritional unit *Calorie* (Cal) is actually a kilocalorie (kcal): 
  \[
  1 \text{ Cal} = 1 \text{ kcal} = 1000 \text{ cal} = 4184 \text{ J}
  \]

**Examples: Kinetic Energy**

1. What is the kinetic energy (in kJ) of a 2300. lb car moving at 55.0 mi/h?

**Answer:** 315 kJ

**Internal Energy, \( E \), and State Functions**

- The *internal energy* (\( E \)) of a system is the sum of all the kinetic and potential energies for every particle in the system.
- The internal energy is a *state function*, which is dependent only on the present state of the system, and not on the pathway by which it got to that state.
  - Some examples of state functions include energy (and many other thermodynamic terms), pressure, volume, altitude, distance, etc.
- An energy change in a system can occur by many *pathways* (different combinations of heat and work), but no matter what the combination, \( \Delta E \) is always the same — the *amount* of the energy change does not depend on *how* the change takes place.
State Functions

Change in altitude is a state function: it only depends on the difference between the initial and final values, not on the path that the climbers take.

Figure 5.2

State Function — A Chemical Example

\[ C_8H_{18}(l) + \frac{25}{2} O_2(g) \rightarrow 8CO_2(g) + 9H_2O(g) \]

initial state \( E_{\text{initial}} \) final state \( E_{\text{final}} \)

- For a given change, \( \Delta E (q + w) \) is constant, even though the specific values of \( q \) and \( w \) can vary.
- Heat and work are NOT state functions, but \( \Delta E \) is.

The System and the Surroundings

- An isolated system does not exchange energy or matter with its surroundings (e.g., an ideal Thermos bottle).
- A closed system exchanges energy but not matter with its surroundings (e.g., a cup of soup with a lid).
- An open system exchanges energy and matter with its surroundings (e.g., a bowl of soup that is open to the air, which can evaporate, or have things added).

Exothermic and Endothermic Processes

- If the system loses energy, the surroundings gain energy, and vice versa. Energy changes are usually considered from the point of view of the system.
  - An exothermic process is one where energy flows out of the system.
  - An endothermic process is one where energy flows into the system.
- A process that is exothermic in one direction (e.g., from gas to liquid) is endothermic in the other direction (from liquid to gas).
The First Law: Conservation of Energy

- The law of conservation of energy, also known as the first law of thermodynamics, states that energy cannot be created or destroyed; it can only be converted from one form into another.
- In other words, the total energy of the universe is a constant.

\[ \Delta E_{\text{universe}} = \Delta E_{\text{system}} + \Delta E_{\text{surroundings}} = 0 \]

- Potential and kinetic energy are interconvertible, but for a particular system the total amount of potential and kinetic energy is a constant.

Change in Internal Energy

- For an isolated system, with no energy flowing in or out of the system, the internal energy is a constant.
  - First Law of Thermodynamics (restated): The total internal energy of an isolated system is constant.
- It is impossible to completely isolate a reaction from its surroundings, but it is possible to measure the change in the internal energy of the system, \( \Delta E \), as energy flows into the system from the surroundings or flows from the system into the surroundings.

\[ \Delta E = E_{\text{final}} - E_{\text{initial}} \]
\[ \Delta E = E_{\text{products}} - E_{\text{reactants}} \]

Energy Flow: Sign Conventions

- By convention, energy changes are measured from the point of view of the system.
  - Any energy that flows from the system to the surroundings has a negative sign:
    \[ E_{\text{final}} < E_{\text{initial}} \]
    \[ \Delta E < 0 \]
  - Any energy that flows to the system from the surroundings has a positive sign:
    \[ E_{\text{final}} > E_{\text{initial}} \]
    \[ \Delta E > 0 \]

Examples: Energy Flow

2. When gasoline burns in a car engine, the heat released causes the products CO\(_2\) and H\(_2\)O to expand, which pushes the pistons outward. Excess heat is removed by the car’s cooling system. If the expanding gases do 451 J of work on the pistons and the system loses 325 J to the surroundings as heat, calculate the change in energy in J, kJ, and kcal.

Answer: -776 J, -0.776 kJ, -0.185 kcal

Work

- Work \((w)\) is defined as the force \((F)\) that produces the movement of an object through a distance \((d)\):
  \[ w = F \times d \]
- Work also has units of J, kJ, cal, kcal, Cal, etc.
- The two most important types of chemical work are:
  - the electrical work done by moving charged particles (which is important in electrochemistry).
  - the expansion work done as a result of a volume change in a system, particularly from an expanding or contracting gas. This is also known as pressure-volume work, or PV work.
Pressure-Volume Work

• When propane, \( \text{C}_3\text{H}_8 \), is burned, 7 moles of gas are produced for every 6 moles of reactants:
  \[
  \text{C}_3\text{H}_8(\text{g}) + 5\text{O}_2(\text{g}) \rightarrow 3\text{CO}_2(\text{g}) + 4\text{H}_2\text{O}(\text{g})
  \]
  – If the reaction takes place in a container with a movable piston, the greater volume of gas product will force the piston outward against the pressure of the atmosphere, thus doing work on the piston.

• **Pressure-volume work** is equal to the pressure \( P \) times the change in volume \( \Delta V \); the sign is negative because work is being done by the system (work energy is leaving the system):
  \[
  w = -P\Delta V
  \]
  – The units of PV work are \( \text{L} \cdot \text{atm} \); 1 \( \text{L} \cdot \text{atm} \) = 101.3 J.

Expansion Work

\[
\begin{align*}
\text{V-P work} &= P \cdot \Delta V \\
\text{F/A} &= \text{Pressure} \cdot \text{Area} \\
\text{For a cylinder, V = Ah} \\
\text{w = PAd} \\
\text{w = PAth} \\
\text{w = -PAd}
\end{align*}
\]

3. Calculate the work done (in kJ) during a reaction in which the volume expands from 12.0 \( \text{L} \) to 14.5 \( \text{L} \) against an external pressure of 5.00 atm.

Answer: -1.3 kJ

Energy Changes at Constant Pressure; Enthalpy

• If a process is carried out at constant volume \( (\Delta V = 0) \), the energy change of the reaction appears entirely as heat and not work \( (\Delta E = q - P\Delta V) \).
  – Most reactions are carried out in open vessels at constant pressure, with the volume capable of changing freely.
  – In these cases, \( \Delta V \neq 0 \), and the energy change may be due to both heat transfer and PV work.

• In order to eliminate the contribution from PV work, a quantity called **enthalpy**, \( H \), is defined as internal energy \( (E) \) plus the product of pressure and volume:
  \[
  H = E + PV
  \]
  \[
  \Delta H = \Delta E + P\Delta V
  \]
Energy Changes at Constant Pressure; Enthalpy

- By doing a little algebra, we can see the relationship between $\Delta H$ and energy:
  \[ \Delta E_{\text{rxn}} = q + w \]
  \[ \Delta E_{\text{rxn}} = q - P\Delta V \]
  \[ \Delta H = \Delta E + P\Delta V \]
  \[ \Delta H = (q - P\Delta V) + P\Delta V \]
  \[ \Delta H = q_p \]
- Therefore, the change in enthalpy equals the heat evolved at constant pressure, $q_p$.
- The enthalpy change, $\Delta H$, is also called the heat of reaction for the process. It is also a state function:
  \[ \Delta H = H_{\text{final}} - H_{\text{initial}} = H_{\text{products}} - H_{\text{reactants}} \]

Exothermic vs. Endothermic Processes

- A chemical reaction can either release or absorb heat energy:
  - An endothermic process absorbs heat energy and results in an increase in the enthalpy of the system (the products have more enthalpy than the reactants).
  - An exothermic process releases heat energy and results in a decrease in the enthalpy of the system (the products have less enthalpy than the reactants).
  \[ H_{\text{final}} < H_{\text{initial}} \quad \Delta H < 0 \quad \text{exothermic} \]
  \[ H_{\text{final}} > H_{\text{initial}} \quad \Delta H > 0 \quad \text{endothermic} \]

Where Does the Energy Come From?

- When an exothermic reaction occurs, the chemical potential energy that used to be stored in the chemical bonds in the reactants.
  - The higher energy bonds break and lower energy bonds form, and the system goes from a higher potential energy to a lower potential energy.
  - The energy difference is usually emitted in the form of heat or light.
- When an endothermic reaction occurs, the energy that is absorbed by the system allows new bonds with higher energies to be formed, and the potential energy of the system is raised.

Enthalpy vs. Energy

- While $\Delta E$ is a measure of the entire energy change of a system (heat and work), $\Delta H$ is a measure of only the heat exchanged at constant pressure.
- Most reactions do take place at constant (i.e., atmospheric) pressure, so $\Delta H$ is a good measure of energy changes in most thermodynamic systems.
  - In reactions that do not involve gases, volume changes are approximately zero, and $\Delta H \approx \Delta E$.
  - When the number of moles of gas doesn’t change, $\Delta V = 0$, and $\Delta H = \Delta E$.
  - Even in reactions in which the number of moles of gas does change, $q_P$ is usually much larger than $P\Delta V$, so $\Delta H \approx \Delta E$.

Enthalpy Diagrams

Thermochemical Equations

- A thermochemical equation is a balanced equation that also states the heat of reaction ($\Delta H$).
- The reaction of 1 mole of $N_2$ and 3 moles of $H_2$ to form 2 moles of $NH_3$ releases 92.38 kJ of energy:
  \[ N_2(g) + 3H_2(g) \rightarrow 2NH_3(g); \Delta H = -92.38 \text{ kJ} \]
  - This $\Delta H$ value is true only when the coefficients are taken to mean the number of actual moles they express for that particular reaction, with the reagents in those particular physical states.
  - For other amounts of reactants or products, the energy change of the reaction can be calculated by using the $\Delta H$ term in the same way that the coefficients are used.
Examples: Thermochemical Equations

1. How much heat (in kJ) is evolved when 5.00 g of aluminum reacts with a stoichiometric amount of Fe$_2$O$_3$ in the thermite reaction?

2Al(s) + Fe$_2$O$_3$(s) → 2Fe(s) + Al$_2$O$_3$(s); $\Delta H^\circ = -852$ kJ

Answer: 78.8 kJ

MOV: Thermite

Examples: Thermochemical Equations

2. If aluminum is produced by the thermal decomposition of bauxite (mostly Al$_2$O$_3$), how many grams of Al can form when 1.000 $\times$ 10$^3$ kJ of heat is transferred?

Al$_2$O$_3$(s) → 2Al(s) $+ \frac{3}{2}$O$_2$(g); $\Delta H = +1676$ kJ

Answer: 32.20 g Al

Manipulating Thermochemical Equations

- If a chemical equation is multiplied by some factor, then $\Delta H_{rxn}$ is multiplied by the same factor.

2H$_2$(g) + O$_2$(g) → 2H$_2$O(g); $\Delta H = -483.6$ kJ

4H$_2$(g) + 2O$_2$(g) → 4H$_2$O(g); $\Delta H = -967.2$ kJ

H$_2$(g) $+ \frac{1}{2}$O$_2$(g) → H$_2$O(g); $\Delta H = -241.8$ kJ

- If a chemical equation is reversed, the sign of $\Delta H_{rxn}$ is reversed. (This is equivalent to multiplying the equation by -1.)

2H$_2$O(g) → 2H$_2$(g) $+ \frac{3}{2}$O$_2$(g); $\Delta H = +483.6$ kJ

H$_2$O(g) → H$_2$(g) $+ \frac{1}{2}$O$_2$(g); $\Delta H = +241.8$ kJ

Examples: Thermochemical Equations

1. Given the following thermochemical equation

N$_2$(g) + 3H$_2$(g) → 2NH$_3$(g); $\Delta H_{rxn} = -92.38$ kJ

What is the $\Delta H_{rxn}$ for the reactions shown below?

a. 2NH$_3$(g) → N$_2$(g) + 3H$_2$(g); $\Delta H = +92.38$ kJ
b. 2N$_2$(g) + 6H$_2$(g) → 4NH$_3$(g); $\Delta H = -184.8$ kJ
c. $\frac{1}{2}$N$_2$(g) $+ \frac{3}{2}$H$_2$(g) → NH$_3$(g); $\Delta H = -46.19$ kJ
d. 4NH$_3$(g) → 2N$_2$(g) $+ 6$H$_2$(g); $\Delta H = +184.8$ kJ
e. 6NH$_3$(g) → 3N$_2$(g) $+ 9$H$_2$(g); $\Delta H = +277.1$ kJ
f. 2NH$_3$(aq) → N$_2$(g) $+ 3$H$_2$(g); $\Delta H = \text{no relation!}$

Examples: Thermochemical Equations

1. Given the following thermochemical equation

C(s) + O$_2$(g) → CO$_2$(g); $\Delta H^\circ = -393.5$ kJ

We can imagine two paths leading from 1 mole of carbon and oxygen (O$_2$) to 1 mole of carbon dioxide:

One-Step Path:

C(s) + O$_2$(g) → CO$_2$(g); $\Delta H^\circ = -393.5$ kJ

Two-Step Path:

C(s) $+ \frac{1}{2}$O$_2$(g) → CO(g); $\Delta H^\circ = -110.5$ kJ

CO(g) $+ \frac{1}{2}$O$_2$(g) → CO$_2$(g); $\Delta H^\circ = -283.0$ kJ

Two Paths to CO$_2$

Hess’s Law and Heats of Formation
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**Enthalpy Diagram for the Formation of CO₂**

\[ \text{C(s) + O}_2(g) \rightarrow \text{CO}_2(g); \quad \Delta H^\circ = -393.5 \text{ kJ} \]

\[ \text{CO(g) + } \frac{1}{2}\text{O}_2(g) \rightarrow \text{CO}_2(g); \quad \Delta H^\circ = -283.0 \text{ kJ} \]

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**Examples: Hess’s Law**

2. Calculate the value of \( \Delta H^\circ \) for the hypothetical reaction:

\[ 2A \rightarrow 3D \]

Use the following equations to determine the value of \( \Delta H^\circ \):

- \( A \rightarrow B; \Delta H^\circ = +10 \text{ kJ} \)
- \( 3C \rightarrow 2B; \Delta H^\circ = -40 \text{ kJ} \)
- \( D \rightarrow C; \Delta H^\circ = -20 \text{ kJ} \)

Answer: \(-98 \text{ kJ}\)

3. Hydrogen peroxide, \( \text{H}_2\text{O}_2 \), decomposes into water and oxygen by the following equation:

\[ \text{H}_2\text{O}_2(l) \rightarrow \text{H}_2\text{O}(l) + \frac{1}{2}\text{O}_2(g); \quad \Delta H^\circ = -188 \text{ kJ} \]

Use the following equations to determine the value of \( \Delta H^\circ \) for the decomposition of hydrogen peroxide:

- \( \text{H}_2(g) + \frac{1}{2}\text{O}_2(g) \rightarrow \text{H}_2\text{O}(l); \Delta H^\circ = -286 \text{ kJ} \)

Answer: \(-98 \text{ kJ}\)

4. Carbon monoxide is often used in metallurgy to remove oxygen from metal oxides and thereby give the free metal. The thermochemical equation for the reaction of CO with iron(III) oxide, \( \text{Fe}_2\text{O}_3 \), is

\[ \text{Fe}_2\text{O}_3(s) + 3\text{CO}(g) \rightarrow 2\text{Fe}(s) + 3\text{CO}_2(g); \quad \Delta H^\circ = -26.7 \text{ kJ} \]

Use this equation and the equation for the combustion of carbon monoxide,

\[ \text{CO}(g) + \frac{1}{2}\text{O}_2(g) \rightarrow \text{CO}_2(g); \quad \Delta H^\circ = -283.0 \text{ kJ} \]

to calculate the value of \( \Delta H^\circ \) for the following reaction:

\[ 2\text{Fe}(s) + \frac{3}{2}\text{O}_2(g) \rightarrow \text{Fe}_2\text{O}_3(s) \]

Answer: \(-822.3 \text{ kJ}\)

5. Use Hess’s law to calculate the value of \( \Delta H^\circ \) for the reaction of tungsten with carbon:

\[ \text{W}(s) + \text{C}(s) \rightarrow \text{WC}(s) \]

Use the following thermochemical equations:

- \( 2\text{W}(s) + 3\text{O}_2(g) \rightarrow 2\text{WO}_3(s); \Delta H^\circ = -1680.6 \text{ kJ} \)
- \( \text{C}(s) + \text{O}_2(g) \rightarrow \text{CO}_2(g); \Delta H^\circ = -393.5 \text{ kJ} \)
- \( 2\text{WC}(s) + 5\text{O}_2(g) \rightarrow 2\text{WO}_3(s) + 2\text{CO}_2(g); \Delta H^\circ = -2391.6 \text{ kJ} \)

Answer: \(-38.0 \text{ kJ}\)
**Thermodynamic Standard States**

- The enthalpy change is the amount of heat released or absorbed when reactants are converted to products at the same temperature and in the molar amounts represented by coefficients in the balanced equation. The physical states must also be specified, since a substance in the gas phase has a different heat content from one in the liquid phase.
- In order to compare thermodynamic measurements from different reactions, a set of conditions called the **thermodynamic standard state** is defined: the most stable form of a substance at 1 atm pressure and 25°C, 1 M for all substances in solution.
- When $\Delta H$ is measured with all substances in their standard states, it is called the **standard enthalpy (heat) of reaction**, $\Delta H^\circ$.

**Standard Enthalpy of Formation ($\Delta H_f^\circ$)**

- The **standard enthalpy (heat) of formation**, $\Delta H_f^\circ$, is the enthalpy change for the formation of 1 mole of a substance in its standard state from its constituent elements in their standard states.
- The most stable form of any element in its standard state is defined: the most stable form of a substance at 1 atm pressure and 25°C, 1 M for all substances in solution.
- When $\Delta H$ is measured with all substances in their standard states, it is called the **standard enthalpy (heat) of reaction**, $\Delta H^\circ$.
- In most cases, $\Delta H_f^\circ$ for a compound is negative (i.e., a compound is usually more stable than its elements.)

**Determining $\Delta H^\circ$ from $\Delta H_f^\circ$**

- The standard enthalpy of reaction can be calculated by subtracting the sum of the heats of formation of all reactants from the sum of the heats of formation of all products, with each $\Delta H_f^\circ$ multiplied by the appropriate coefficient in the balanced equation:

$$n_r \text{ reactants } \rightarrow n_p \text{ products}$$

$$\Delta H^\circ_{rxn} = \sum n_p \Delta H_f^\circ \text{(products)} - \sum n_r \Delta H_f^\circ \text{(reactants)}$$

- This process is really an application of Hess’s Law.
- Thus, to calculate the $\Delta H^\circ$ for any reaction, we write the balanced equation, and look up the $\Delta H_f^\circ$’s of all of the reactants and products.

**Some Important Types of Enthalpy Change**

- **Heat of fusion** ($\Delta H_{fus}$) — enthalpy change when 1 mole of a substance melts.
  
  $$\text{H}_2\text{O(s)} \rightarrow \text{H}_2\text{O(l)}; \Delta H = 6.01 \text{ kJ/mol at } 0°C$$

- **Heat of vaporization** ($\Delta H_{vap}$) — enthalpy change when 1 mole of a substance vaporizes.
  
  $$\text{H}_2\text{O(l)} \rightarrow \text{H}_2\text{O(g)}; \Delta H = 40.7 \text{ kJ/mol at } 100°C$$

- **Heat of sublimation** ($\Delta H_{sub}$) — enthalpy change when 1 mole of a substance sublimes (converts directly from the solid phase to the vapor phase).

- **Heat of combustion** ($\Delta H_c$) — enthalpy change when 1 mole of a substance combines with $O_2$ in a combustion reaction.
  
  $$C_6\text{H}_6(l) + \frac{1}{2}O_2(g) \rightarrow 4\text{CO}_2(g) + 5\text{H}_2\text{O(l)}$$

**Examples: Standard Heats of Formation**

6. Which of the following reactions represent a $\Delta H_f^\circ$ equation?

CO(g) + $\frac{1}{2}O_2(g)$ → CO$_2$(g); $\Delta H_f$ = −283.0 kJ

2H(g) + O(g) → H$_2$O(l); $\Delta H_f$ = −971.1 kJ

2H$_2$(g) + O$_2$(g) → 2H$_2$O(l); $\Delta H_f$ = −571.8 kJ

H$_2$(g) + $\frac{1}{2}O_2(g)$ → H$_2$O(l); $\Delta H_f$ = −285.9 kJ

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**Appendix A4.** Ion pages APP-13 through APP-21 list thermodynamic properties of more substances.
Examples: Standard Heats of Formation

7. What equation must be used to represent the formation of NaHCO₃(s) when we want to include its value of ΔH°?

8. Some chefs keep baking soda, NaHCO₃, handy to put out grease fires. When thrown on the fire, baking soda partly smothers the fire and the heat decomposes it to give CO₂, which further smothers the flame. The equation for the decomposition of NaHCO₃ is

\[ 2\text{NaHCO}_3(s) \rightarrow \text{Na}_2\text{CO}_3(s) + \text{H}_2\text{O}(l) + \text{CO}_2(g) \]

Use the ΔH° data in Appendix A4.3 to calculate the ΔH° for this reaction in kilojoules.

Answer: 91.6 kJ

Examples: Standard Heats of Formation

9. Use the ΔH° data in Appendix A4.3 to calculate ΔH for the combustion of ethanol, C₂H₅OH (l), at 25°C.

Answer: -1234.8 kJ

Examples: Standard Heats of Formation

10. Use the ΔH° data in Appendix A4.3 to calculate the standard heat of vaporization of water.

Answer: +44.0 kJ

Heat Capacity

- The thermal properties of a substance are those that describe its ability to absorb or release heat without changing chemically.
- The heat capacity (C) of an object is the amount of heat (q) required to change its temperature by a given amount (ΔT):

\[ C = \frac{q}{\Delta T} \quad q = C \Delta T \]

\[ \Delta T = T_f - T_i \]

- Heat capacity has units of J/°C (or J/K), and is an extensive property, depending on the sample size.
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**Specific Heat**

- The **specific heat capacity** \((C_s, \text{aka specific heat})\) of an object, is the quantity of heat required to change the temperature of 1 gram of a substance by 1 °C:

\[
C_s = \frac{q}{m \Delta T}
\]

- Specific heat has units of \(\text{J/g °C}\), and is an **intensive** property, which is independent of the sample size.

- The **molar heat capacity** \((C_m)\), is the quantity of heat required to change the temperature of 1 mole of a substance by 1 °C (or K):

\[
C_m = \frac{q}{n \Delta T}
\]

**Examples: Specific Heat**

1. If a gold ring with a mass of 10.00 g changes in temperature from 25.00 °C to 28.00 °C, how much energy in joules has it absorbed? How much energy is absorbed by 10.00 g of \(\text{H}_2\text{O}\) under the same conditions?

Answer: \(q_{\text{Au}} = 3.87 \text{ J}, q_{\text{H}_2\text{O}} = 125 \text{ J}\)

2. What is the specific heat of the (fictional) element dilithium if it takes 2.51 kJ to raise the temperature of 42.0 g of dilithium by 10.0 °C?

Answer: 5.98 J/g °C

3. What is the final temperature of a 100.0 g sample of water initially at 25.0 °C after 25.1 kJ of heat energy is added? (The specific heat of water is 4.18 J/g °C.)

Answer: 85.0 °C

**Heat of Fusion & Heat of Vaporization**

- During a phase change, there is no change in temperature as heat is added, because both physical states are present during a phase change (there is an equilibrium between the two phases).

- The enthalpy change when 1 mole of a solid melts (fuses) into a liquid is called the **heat of fusion**, \(\Delta H_{\text{fus}}\). The enthalpy change during fusion is given by

\[
q = n \Delta H_{\text{fus}}
\]

- The enthalpy change when 1 mole of a liquid vaporizes into a gas is called the **heat of vaporization**, \(\Delta H_{\text{vap}}\). The enthalpy change during vaporization is given by

\[
q = n \Delta H_{\text{vap}}
\]
Heating-Cooling Curves

- A heating-cooling curve shows the changes that occur when heat is added or removed at constant rate from a sample.
  - During a phase change, a change in heat occurs at a constant temperature \( q = n \Delta H_{\text{phase}} \).
  - Within a phase, a change in heat is accompanied by a change in temperature \( q = C, m \Delta T \).

Heating Curve for Water

- Segment 1: Solid ice warms from -25°C to 0°C.
  \[ q = C, \text{ice} \ m \Delta T \]
- Segment 2: Solid ice melts into liquid water at 0°C.
  \[ q = n \Delta H_{\text{fus}} \]
- Segment 3: Liquid water warms from 0°C to 100°C.
  \[ q = C, \text{liquid} \ m \Delta T \]
- Segment 4: Liquid water boils into steam at 100°C.
  \[ q = n \Delta H_{\text{vap}} \]
- Segment 5: Steam warms from 100°C to 125°C.
  \[ q = C, \text{steam} \ m \Delta T \]

Examples: Specific Heat

4. How much energy (in J) is absorbed when 10.0 g of ice melts to form liquid water? (The heat of fusion for water is 6.01 kJ/mol.)

Answer: 3330 J

Examples: Heating Curves

5. How much energy (in kJ) is needed to heat 270. g of ice from -18.0°C to liquid water at 85.0°C? (\( \Delta H_{\text{vap}} = 40.67 \text{ kJ/mol}, \Delta H_{\text{fus}} = 6.01 \text{ kJ/mol} \), the specific heat of ice is 2.03 J g\(^{-1}\) °C\(^{-1}\), the specific heat of liquid water is 4.184 J g\(^{-1}\) °C\(^{-1}\), and the specific heat of steam is 1.865 J g\(^{-1}\) °C\(^{-1}\).)

Answer: 135.7 kJ

Calorimetry

- A calorimeter is an apparatus that is used to measure the energy change that occurs during a chemical or physical process.
- There are two conditions under which calorimetry measurements can be performed:
  - constant-volume calorimetry
  - constant-pressure calorimetry
Chapter 5 Thermochemistry

**Constant-Volume Calorimetry: Measuring ΔE**

\[ \Delta E_{\text{rxn}} = q + w \quad \Delta E_{\text{rxn}} = q - P \Delta V \]

- Under conditions of constant volume, \( \Delta V = 0 \), and therefore \( w = 0 \), and the energy change of the reaction is dependent only on heat evolved at constant volume, \( q_V \):

\[ \Delta E_{\text{rxn}} = q_V \]

- The heat change (and therefore the energy change) in a process occurring at constant volume can be measured in a bomb calorimeter, in which a sample is sealed in a “bomb,” surrounded by a water bath in which the temperature change can be measured precisely.

- Bomb calorimeters are particularly useful in measuring heats of combustion.

**Examples: Constant-Volume Calorimetry**

6. When 1.010 g of sucrose (\( \text{C}_{12}\text{H}_{22}\text{O}_{11} \)) undergoes combustion in a bomb calorimeter, the temperature rises from 24.92 °C to 28.33 °C. Find \( \Delta E_{\text{rxn}} \) for the combustion of sucrose in kJ/mol sucrose. The heat capacity of the bomb calorimeter (determined in a separate experiment) is 4.90 kJ/°C. (You can ignore the heat capacity of the small sample of sucrose because it is negligible compared to the heat capacity of the calorimeter)

Answer: -5660 kJ/mol \( \text{C}_{12}\text{H}_{22}\text{O}_{11} \)

**Constant-Pressure Calorimetry: Measuring ΔH**

- Energy changes at constant pressure are measured in an insulated vessel with a stirrer, thermometer, and a loose-fitting lid that keeps the contents at constant (atmospheric) pressure.

- The data obtained allows us to measure \( \Delta H \).

- (In undergraduate labs, this device is usually approximated by nested coffee cups.)

\[ q_{\text{soln}} = C_{\text{a,soln}} m_{\text{soln}} \Delta T \]

\[ q_{\text{soln}} = -q_{\text{soln}} \]

**Examples: Constant-Pressure Calorimetry**

7. A 25.64 g sample of a solid was heated in a test tube to 100.00 °C in boiling water and carefully added to a coffee-cup calorimeter containing 50.00 g water. The water temperature increased from 25.10 °C to 28.49 °C. What is the specific heat capacity of the solid? (Assume all the heat is gained by the water.)

Answer: 0.387 J/g°C

**Examples: Constant-Pressure Calorimetry**

8. The reaction of hydrochloric acid and sodium hydroxide is exothermic. The equation is

\[ \text{HCl(aq)} + \text{NaOH(aq)} \rightarrow \text{NaCl(aq)} + \text{H}_2\text{O(l)} \]

In one experiment, a student placed 50.0 mL of 1.00 \( M \) HCl at 25.50 °C in a coffee cup calorimeter. To this was added 50.0 mL of 1.00 \( M \) NaOH solution also at 25.50 °C. The mixture was stirred, and the temperature quickly increased to a maximum of 32.40 °C. What is the energy evolved in kilojoules per mole of HCl? (Because the solutions are relatively dilute, we can assume that their specific heats are close to that of water, 4.18 J g⁻¹ °C⁻¹, and that their densities are 1.00 g mL⁻¹.)

Answer: 57.8 kJ/mol